



# Multi-GNSS Opportunities and Challenges

Never Stand Still

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# Multi-GNSS

## Opportunities and Challenges

- Introduction
- Opportunities
- Challenges and Solutions
- Concluding remarks

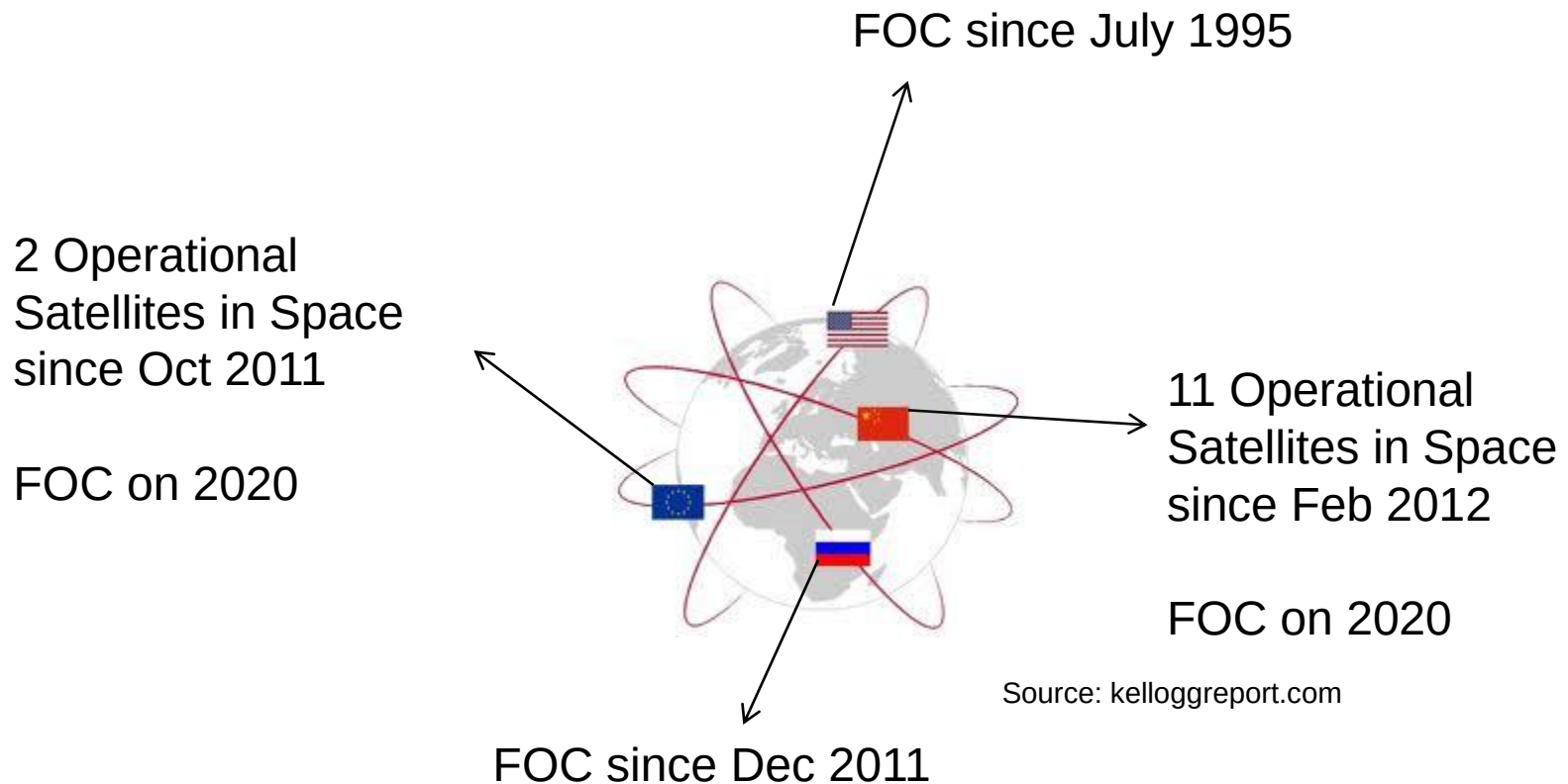
# Introduction

GLONASS  
FOC on  
08/12/2011



Source: gislounge.com

# Introduction



<http://www.colorado.edu/geography/gcraft/notes/gps/foc.txt>

<http://www.glonass-ianc.rsa.ru/en/>

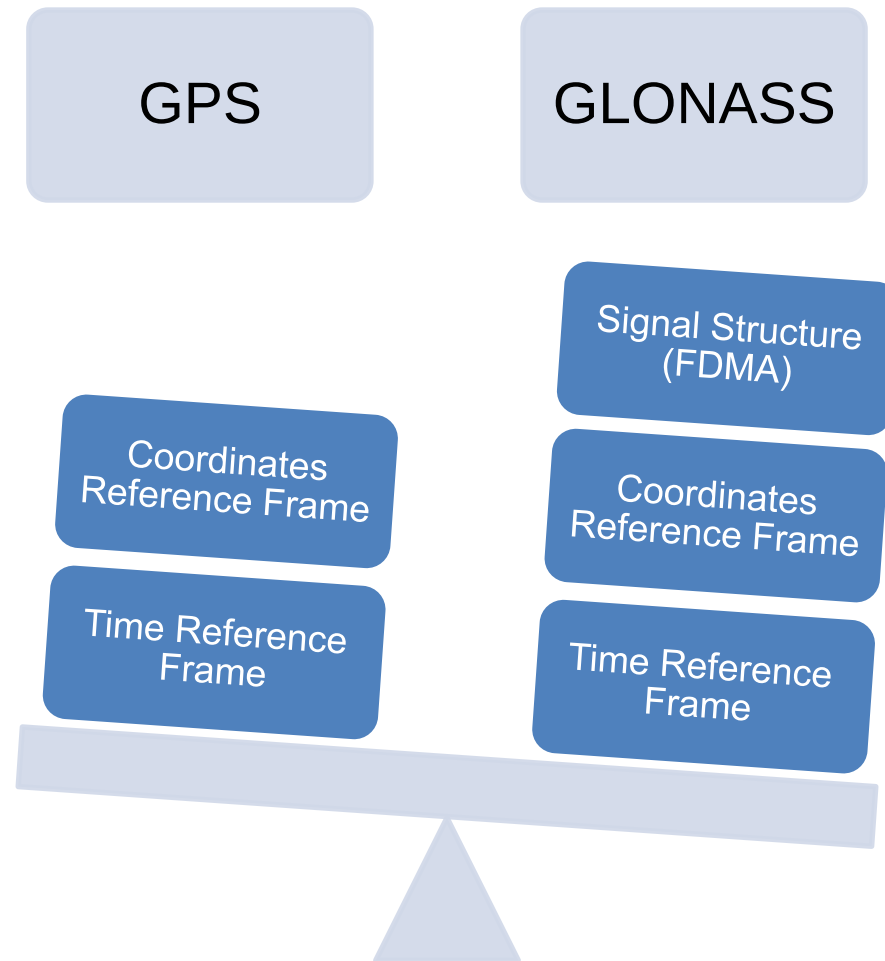
<http://www.beidou.gov.cn/xtjs.html>

<http://www.esa.int/esaNA/galileo.html>

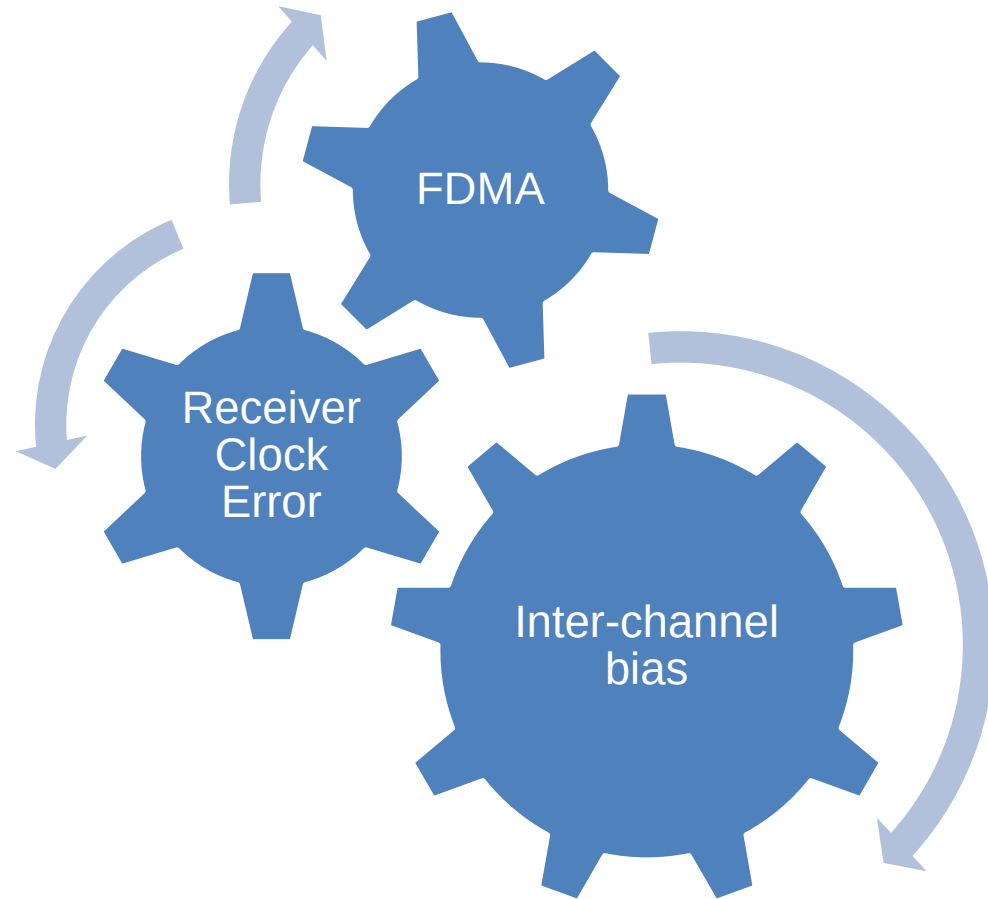
# Opportunities

- Number of visible satellites increase >>> satellite geometry improves >>> positioning accuracy improves
- Increasing availability of GLONASS products from IGS analysis centres >>> real-time application becomes possible
- More and more GPS+GLONASS CORS networks >>> precise GNSS applications in post-mission and real-time

# Challenges



# Challenges



# Receiver Clock Error

- Estimation

- System 1

$$P_{rm,1}^{GPS,pq} = \rho_{rm,1}^{pq} + \varepsilon_{rm,1}^{pq}$$

$$P_{rm,1}^{GLO,x} = \rho_{rm,1}^x + cdt_{rm} + \varepsilon_{rm,1}^x$$

$$\phi_{rm,1}^{GPS,pq} = \frac{f_1}{c} \rho_{rm,1}^{pq} + N_{rm,1}^{pq} + \tau_{rm,1}^{pq}$$

$$\phi_{rm,1}^{GLO,xy} = \frac{f_1^x}{c} \rho_{rm,1}^x - \frac{f_1^y}{c} \rho_{rm,1}^y + \left( \frac{f_1^x}{c} - \frac{f_1^y}{c} \right) cdt_{rm} + N_{rm,1}^{xy} + \tau_{rm,1}^{xy}$$

- Elimination

- System 2

$$P_{rm,1}^{GPS,pq} = \rho_{rm,1}^{pq} + \varepsilon_{rm,1}^{pq}$$

$$P_{rm,1}^{GLO,xy} = \rho_{rm,1}^{xy} + \varepsilon_{rm,1}^{xy}$$

$$\Phi_{rm,1}^{GPS,pq} = \rho_{rm,1}^{pq} + \frac{c}{f_1} N_{rm,1}^{pq} + \tau_{rm,1}^{pq}$$

$$\Phi_{rm,1}^{GLO,xy} = \rho_{rm,1}^{pq} + \frac{c}{f_1^x} N_{rm,1}^x - \frac{c}{f_1^y} N_{rm,1}^y + \tau_{rm,1}^{xy}$$



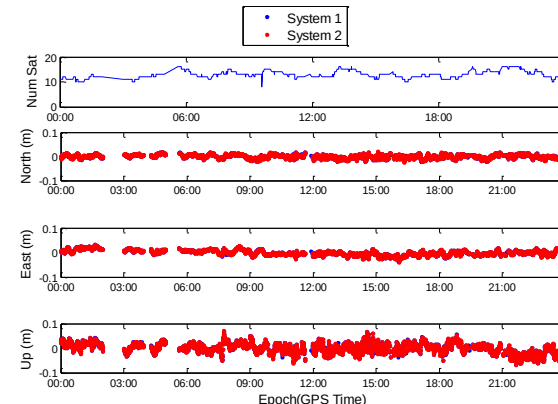
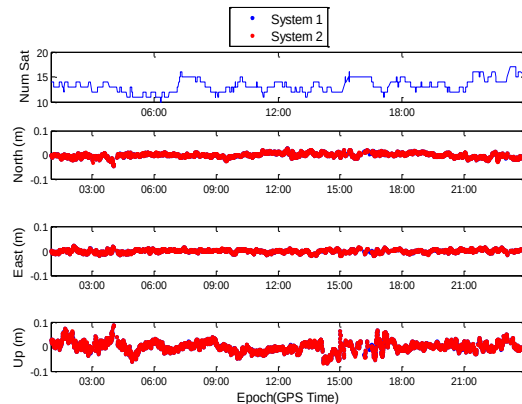
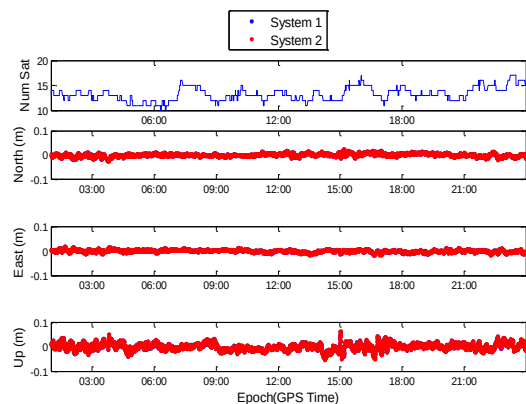
# Receiver Clock Error

## Summary of static RTK test parameters

|                        | CHUN029 | BTRG029 | CHPB029 |
|------------------------|---------|---------|---------|
| <b>Data length</b>     | 24 hr   | 24hr    | 24hr    |
| <b>Obs. Type</b>       | L1+L2   | L1+L2   | L1+L2   |
| <b>Baseline Length</b> | 4.4km   | 8.3km   | 9.7km   |
| <b>Receiver Types</b>  | Leica   | Trimble | Leica   |
| <b>Elevation mask</b>  | 15°     | 15°     | 15°     |
| <b>Interval</b>        | 15s     | 15s     | 15s     |

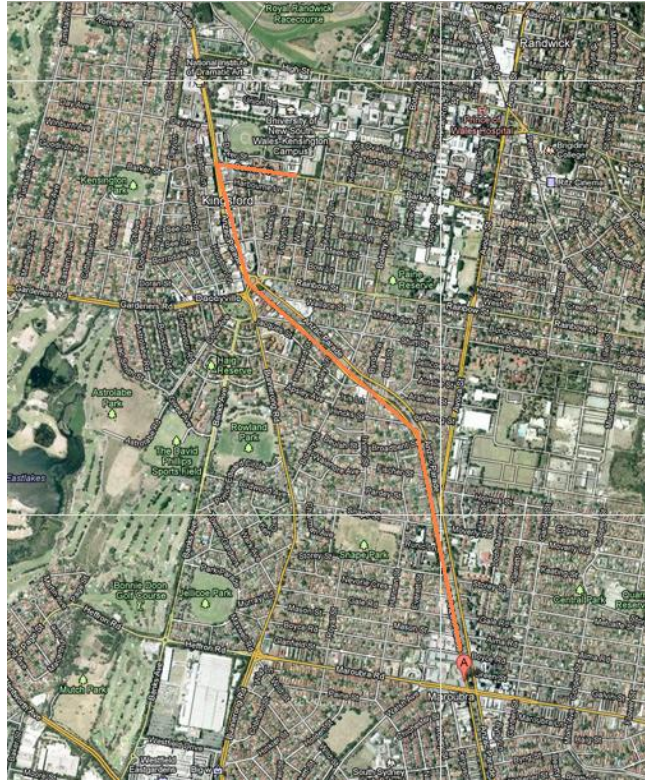
(29\12\2011)

# Receiver Clock Error



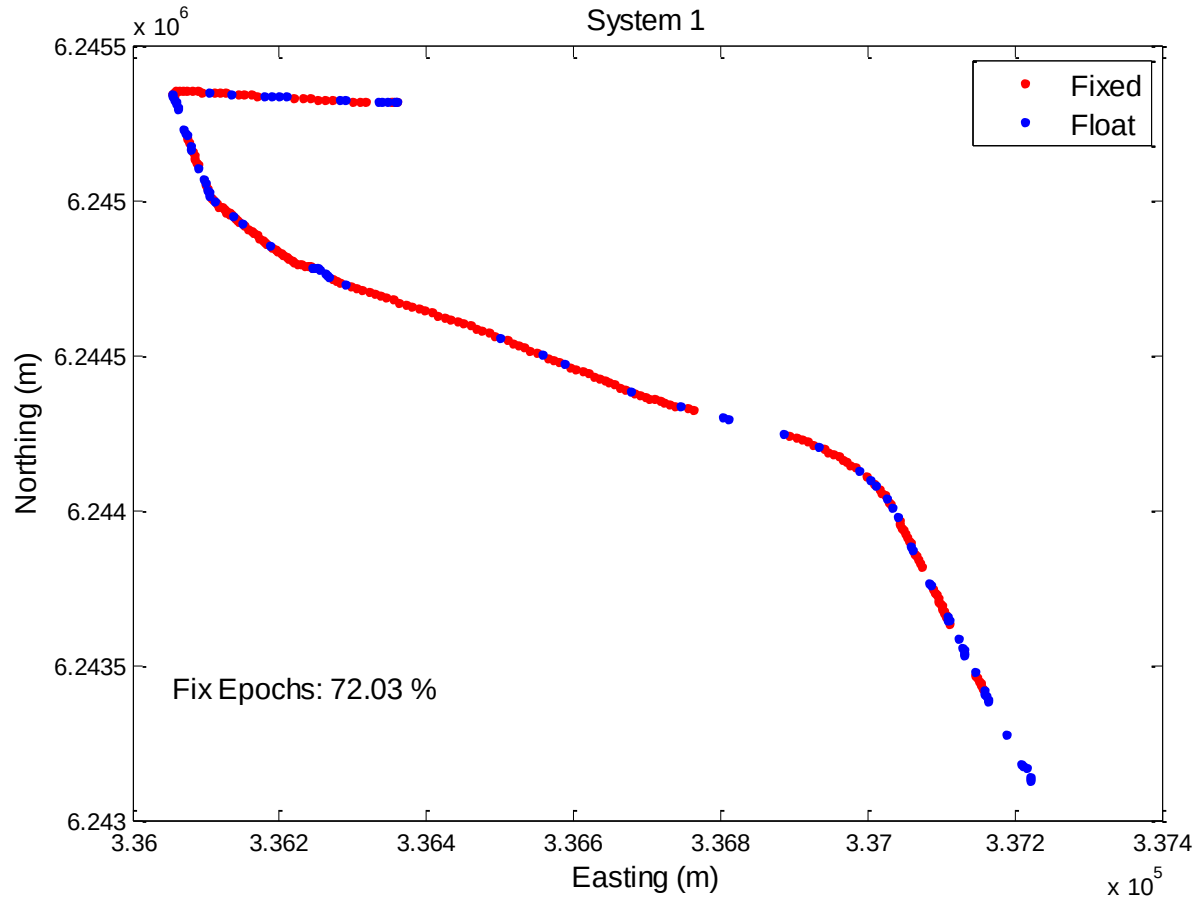
| <i>Baseline</i> | <i>GPS-GLO<br/>model</i> | <i>Standard deviation (m)</i> |       |       |
|-----------------|--------------------------|-------------------------------|-------|-------|
|                 |                          | E                             | N     | U     |
| <b>CHUN029</b>  | System 1                 | 0.006                         | 0.005 | 0.013 |
|                 | System 2                 | 0.006                         | 0.005 | 0.013 |
| <b>BTRG060</b>  | System 1                 | 0.007                         | 0.010 | 0.021 |
|                 | System 2                 | 0.007                         | 0.010 | 0.021 |
| <b>CHPB029</b>  | System 1                 | 0.008                         | 0.006 | 0.019 |
|                 | System 2                 | 0.008                         | 0.006 | 0.019 |

# Receiver Clock Error

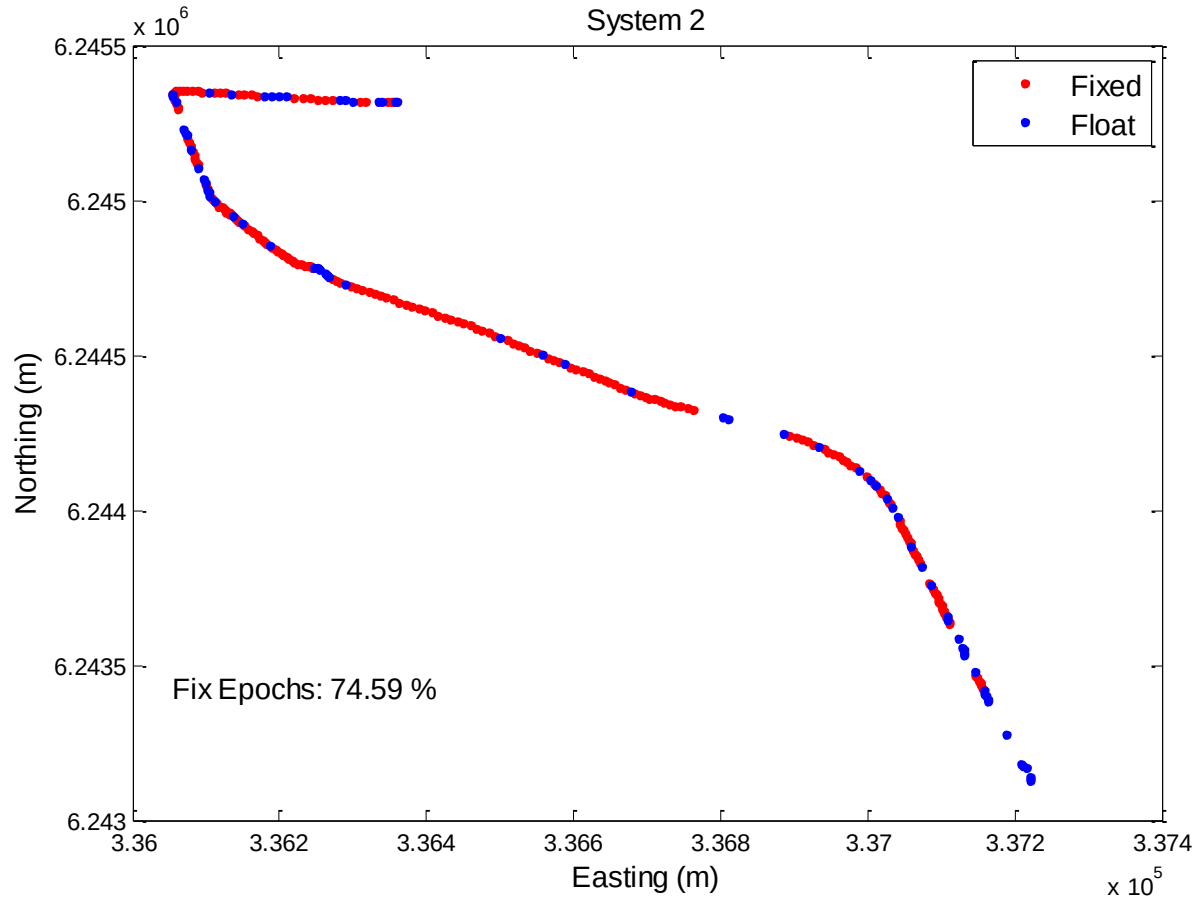


(21\12\2011)

# Receiver Clock Error



# Receiver Clock Error



# Inter-channel Bias

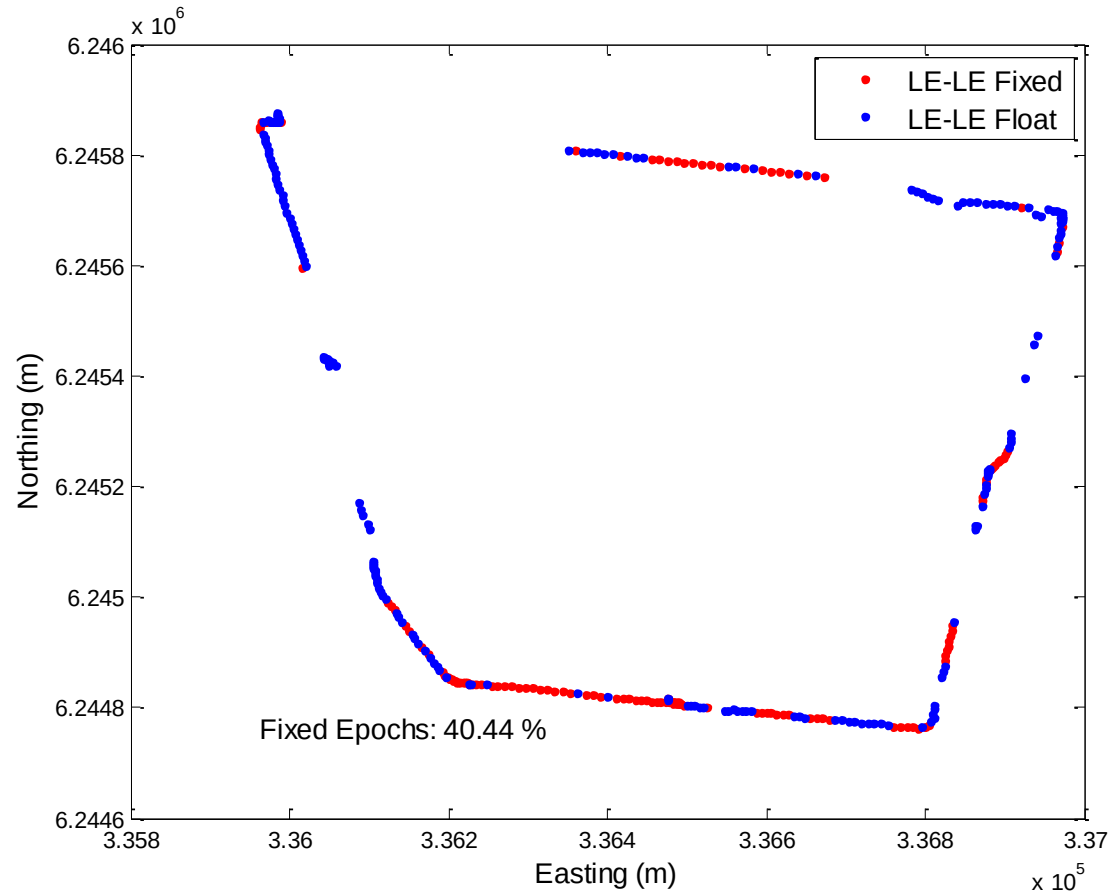
- Identification
- estimation
- calibration

# Inter-channel Bias - Identification



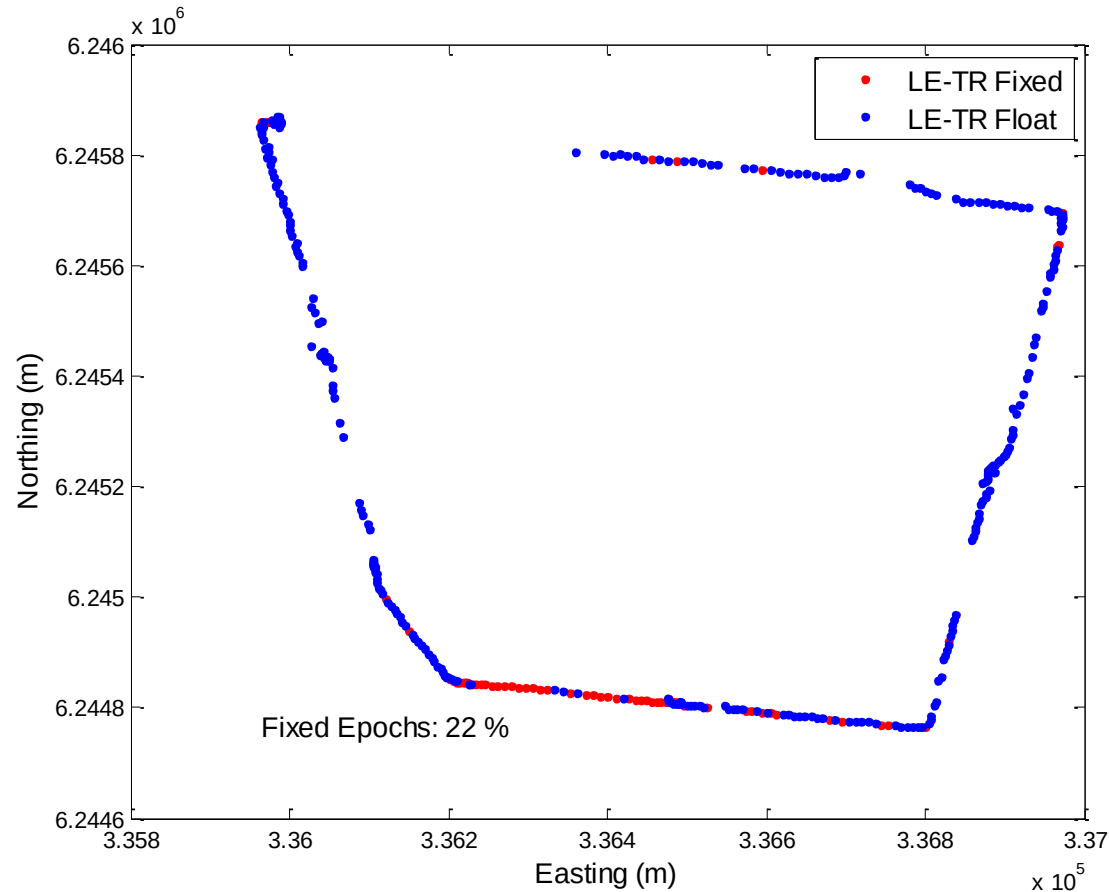
21/12/2011

# Inter-channel Bias - Identification

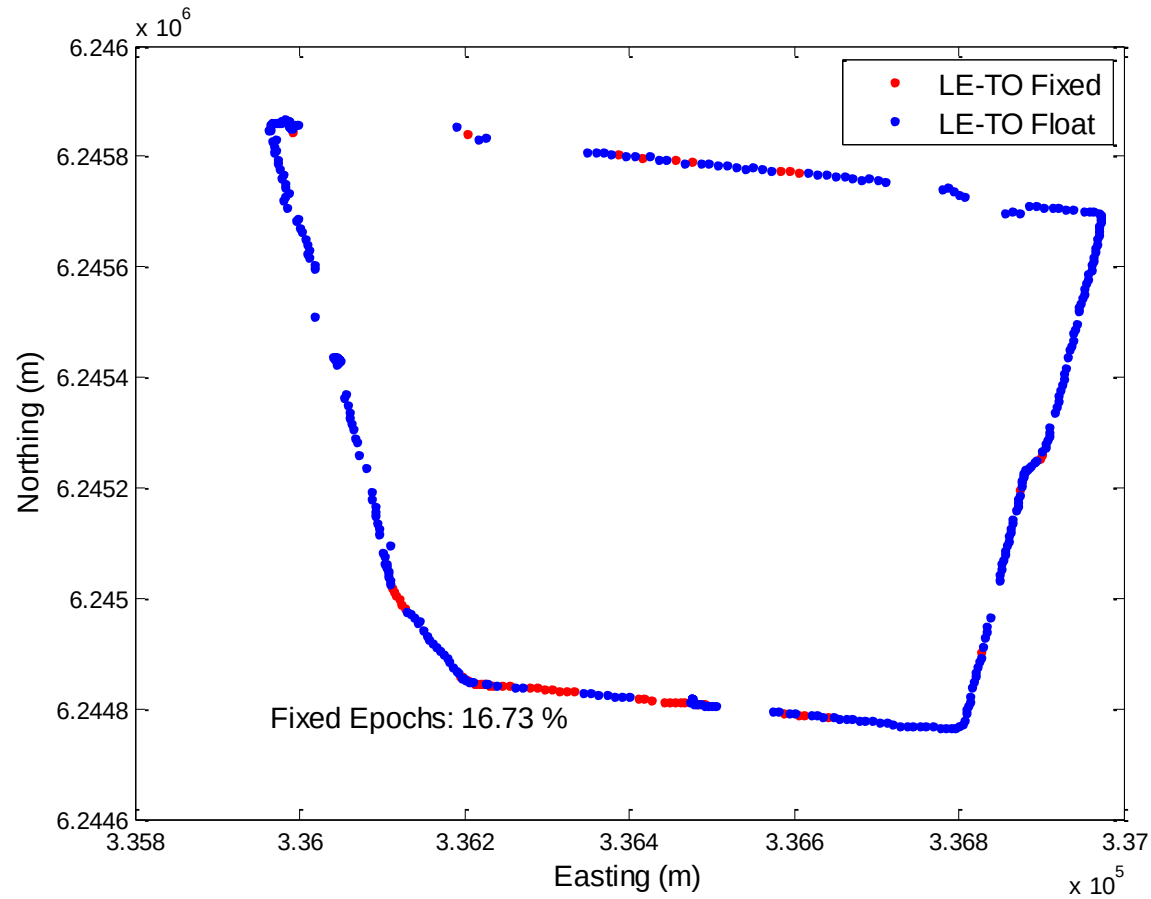




# Inter-channel Bias - Identification



# Inter-channel Bias - Identification



# Inter-channel Bias - Estimation



(29\01\2012), 23hr, 15 sec

# Inter-channel Bias - Estimation

$$P_{rm,1}^{GPS,pq} = \rho_{rm}^{pq} + v_{rm,1}^{pq}$$

$$P_{rm,1}^{GLO,pq} = \rho_{rm}^{pq} + (k^p - k^q) c \zeta_{rm} + v_{rm,1}^{pq}$$

$$\Phi_{rm,1}^{GPS,pq} = \rho_{rm}^{pq} + \frac{c}{f_1} (N_{rm,1}^p - N_{rm,1}^q) + \varepsilon_{rm,1}^{pq}$$

$$\Phi_{rm,1}^{GLO,pq} = \rho_{rm}^{pq} + \frac{c}{f_1^p} N_{rm,1}^p - \frac{c}{f_1^q} N_{rm,1}^q + (k^p - k^q) c \gamma_{rm} + \varepsilon_{rm,1}^{pq}$$

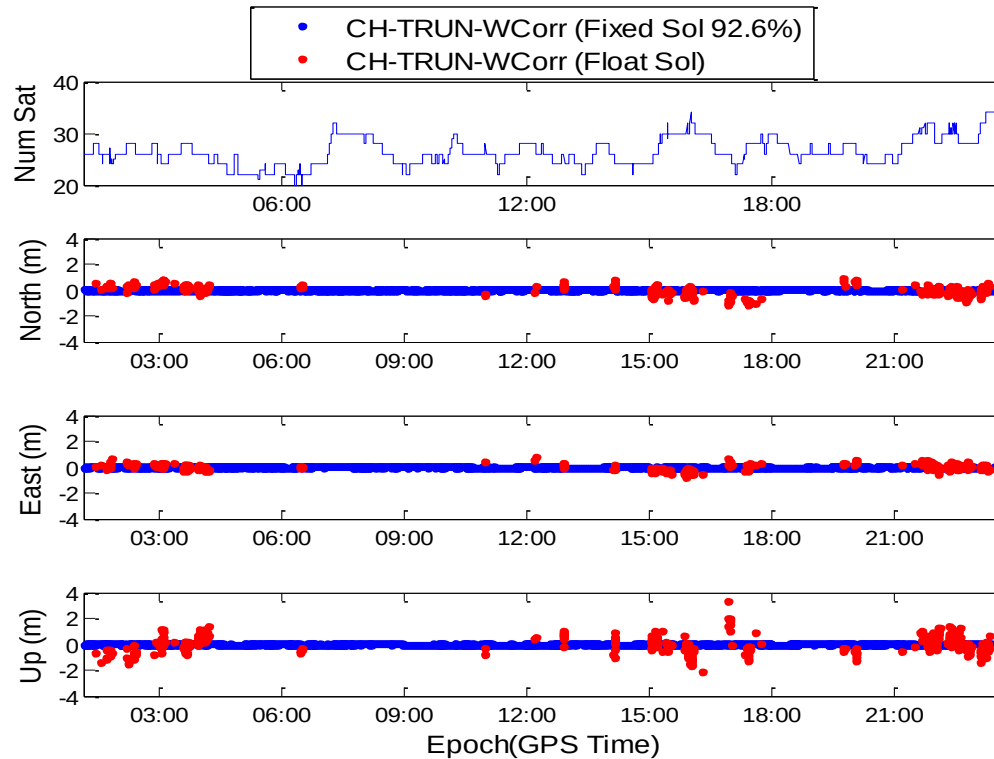
$c\gamma_{rm}$  CPH inter-channel bias expressed in metres by multiplying it by speed of light (c).

$c\zeta_{rm}$  PR inter-channel bias expressed in metres by multiplying it by speed of light (c).

GLONASS channel number for satellite (p) (-7~+6)

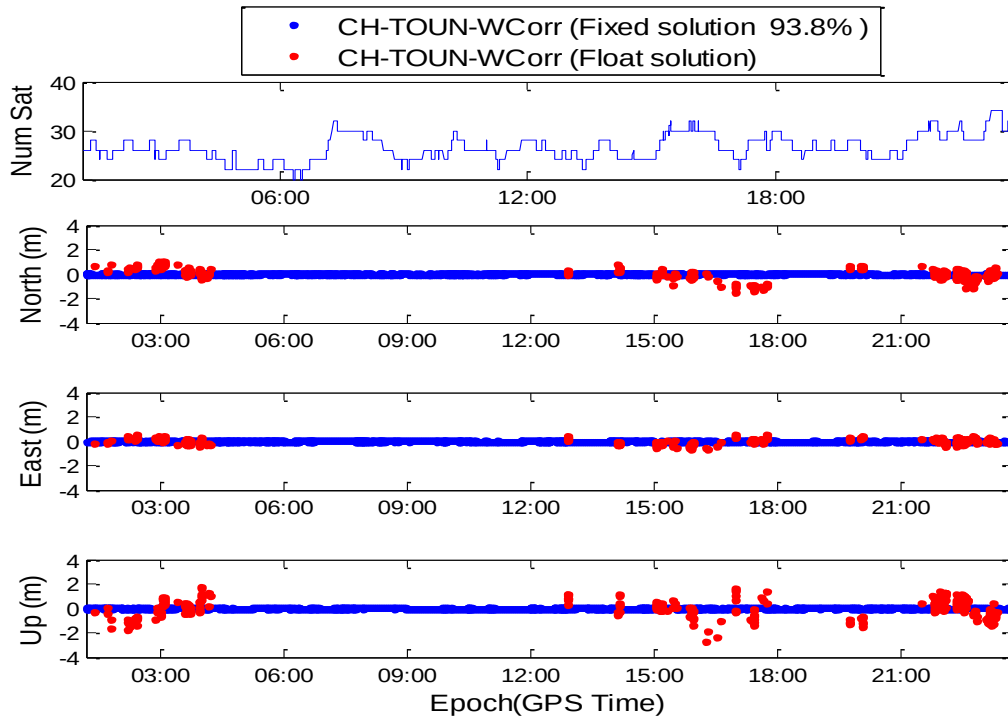
| Average values of inter-channel bias between mixed receivers |                 |                |
|--------------------------------------------------------------|-----------------|----------------|
|                                                              | LEICA - Trimble | LEICA - Topcon |
| CPH (m)                                                      | <b>-0.031</b>   | <b>-0.024</b>  |
| PR (m)                                                       | <b>-0.173</b>   | <b>-0.115</b>  |

# Inter-channel Bias - Calibration



| <i>LEICA-TRIMBLE</i> | <i>Standard deviation (m)</i> |       |       |
|----------------------|-------------------------------|-------|-------|
|                      | E                             | N     | h     |
| With Correction      | 0.006                         | 0.005 | 0.013 |
| Without Correction   | 0.242                         | 0.193 | 0.568 |

# Inter-channel Bias - Calibration



| LEICA-TOPCON       | Standard deviation (m) |       |       |
|--------------------|------------------------|-------|-------|
|                    | E                      | N     | H     |
| With Correction    | 0.006                  | 0.005 | 0.013 |
| Without Correction | 0.344                  | 0.206 | 0.702 |

# Concluding Remarks

- Will these challenges become a real obstacle to an “interoperable GNSS world”?????
  - Receiver clock error is well mitigated
  - Inter-channel bias still needs more attention from GNSS community.
- The answer may rely on a collaboration between GNSS analysis centres-academia-industry.